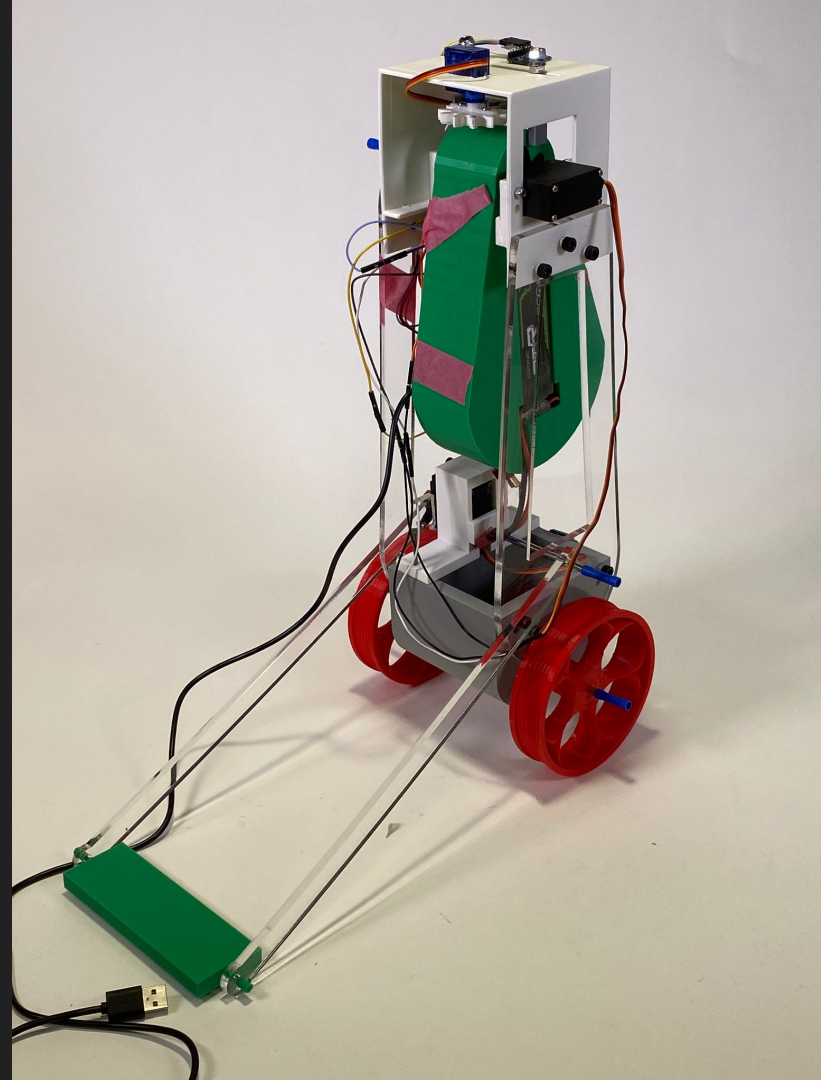


PendulumRoller

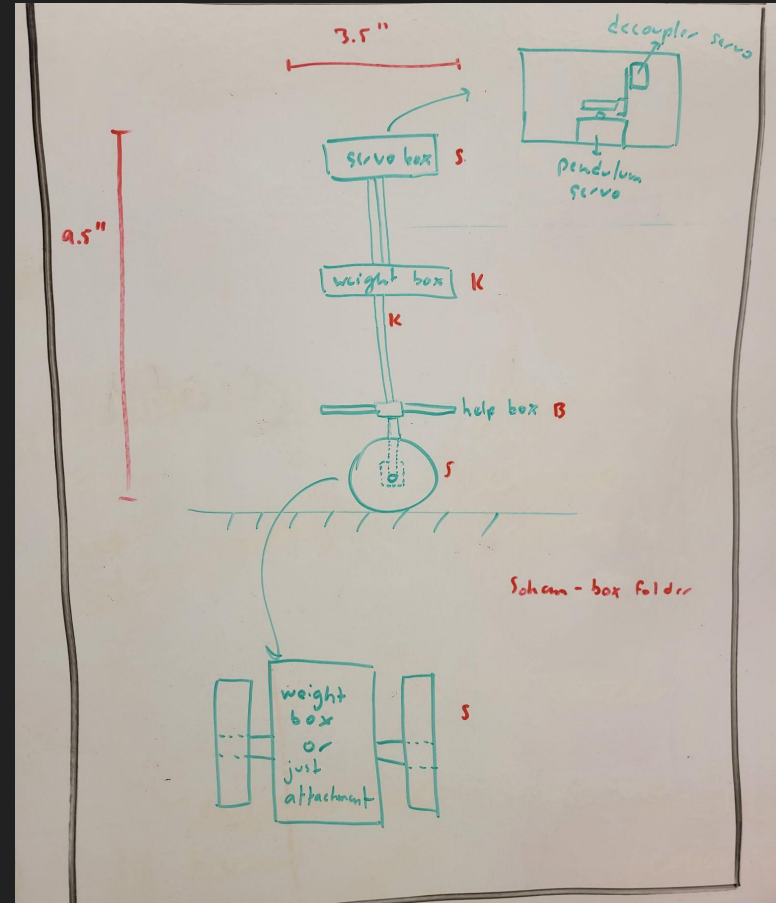
HW 4 Group 2

Kat Allen
Soham Gaggenapally
Benjamin McDermott



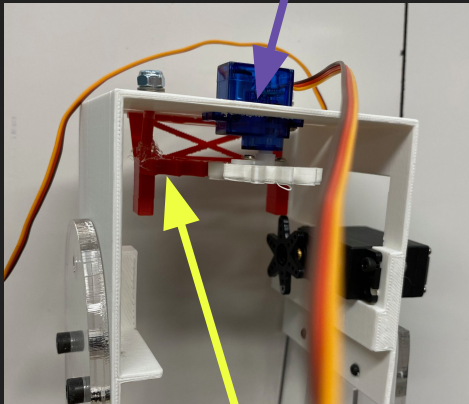
Initial Conception

- Balancing Robot
- Raspberry Pi and battery included onboard near the servos for eas(ier) cable management
- Freewheel on the bottom
- Pendulum driven by servo motor controls balance and motion

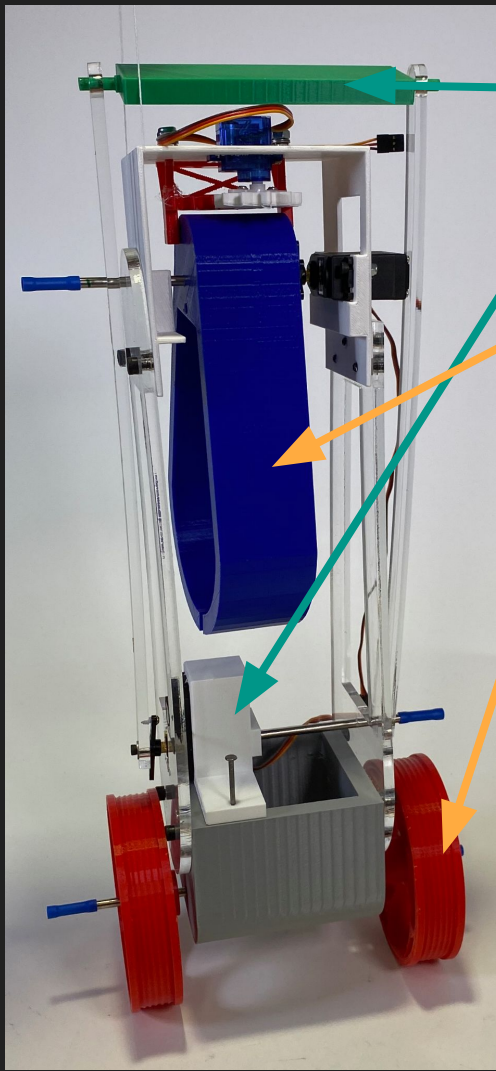


Creativity and Innovation

Vertical Pendulum Decoupler
reduces width of servo box
to allow 90° fall



Alignment Support
simplifies rack and pinion
alignment

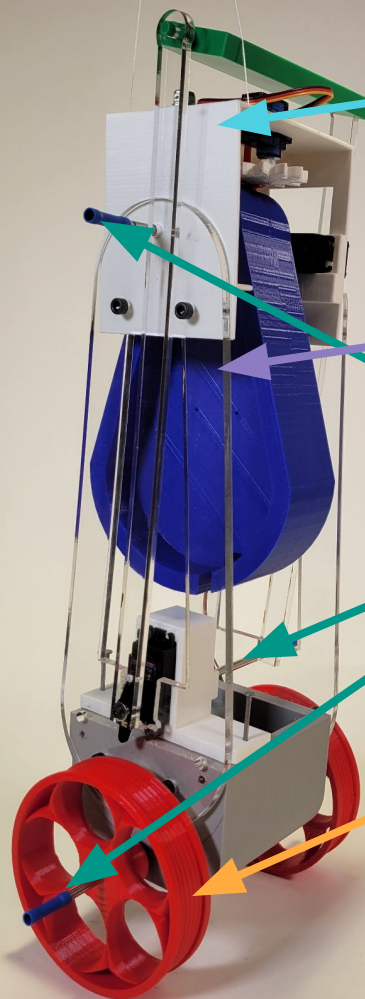


Lifting mechanism
allows fall recovery

Pendulum control and
free-spinning wheels
eliminate the need for
360° servomotors

Onboard storage for
Pi, ESP32 and battery
helps manage cables
and allows them to
double as pendulum
mass





Servo Box

Holds pendulum support, controller and decoupling mechanism

Pendulum

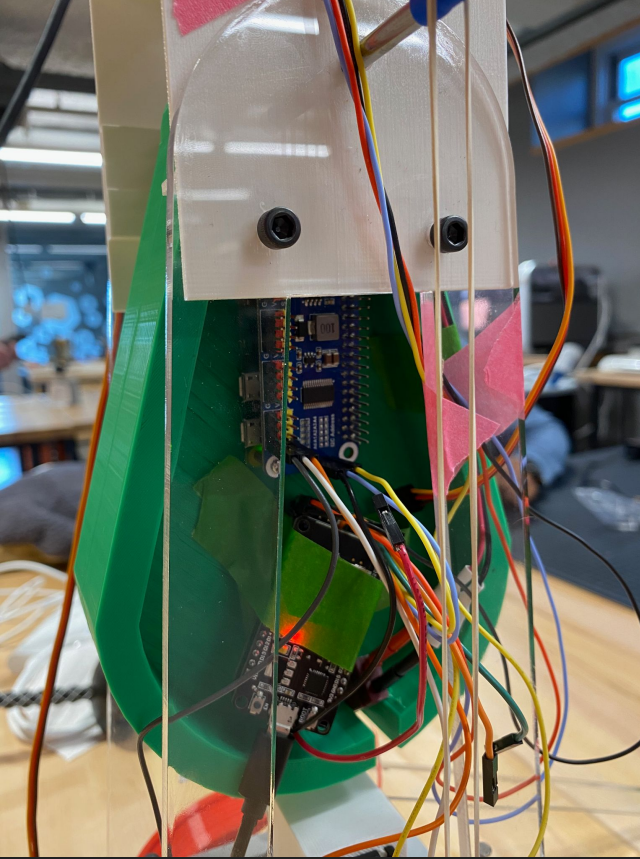
Provides control via rotation to balance, holds electronics and power

Metal Axels allow low-friction rotation for pendulum, wheels, and lifter assembly

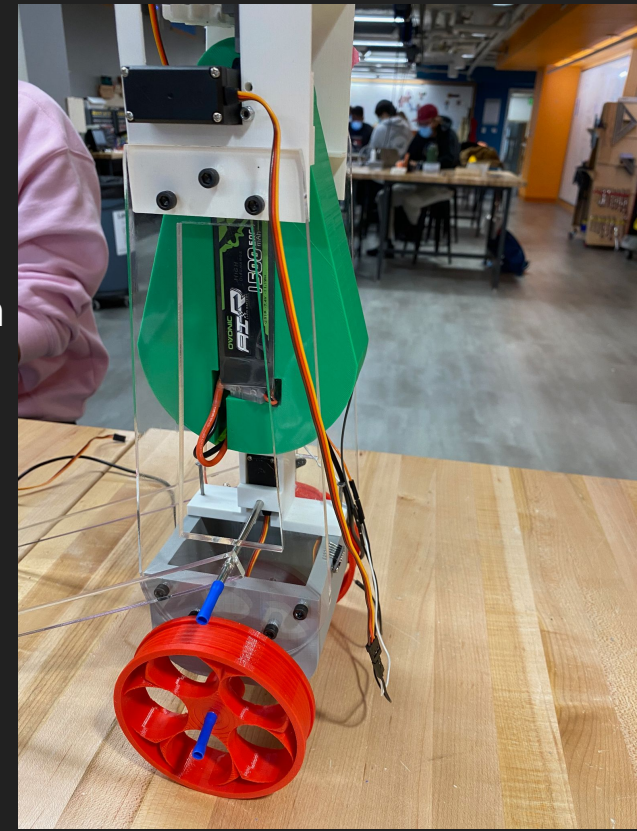
Wide Freewheel Base

Allows free rotation in x-direction, restricts motion in y-direction

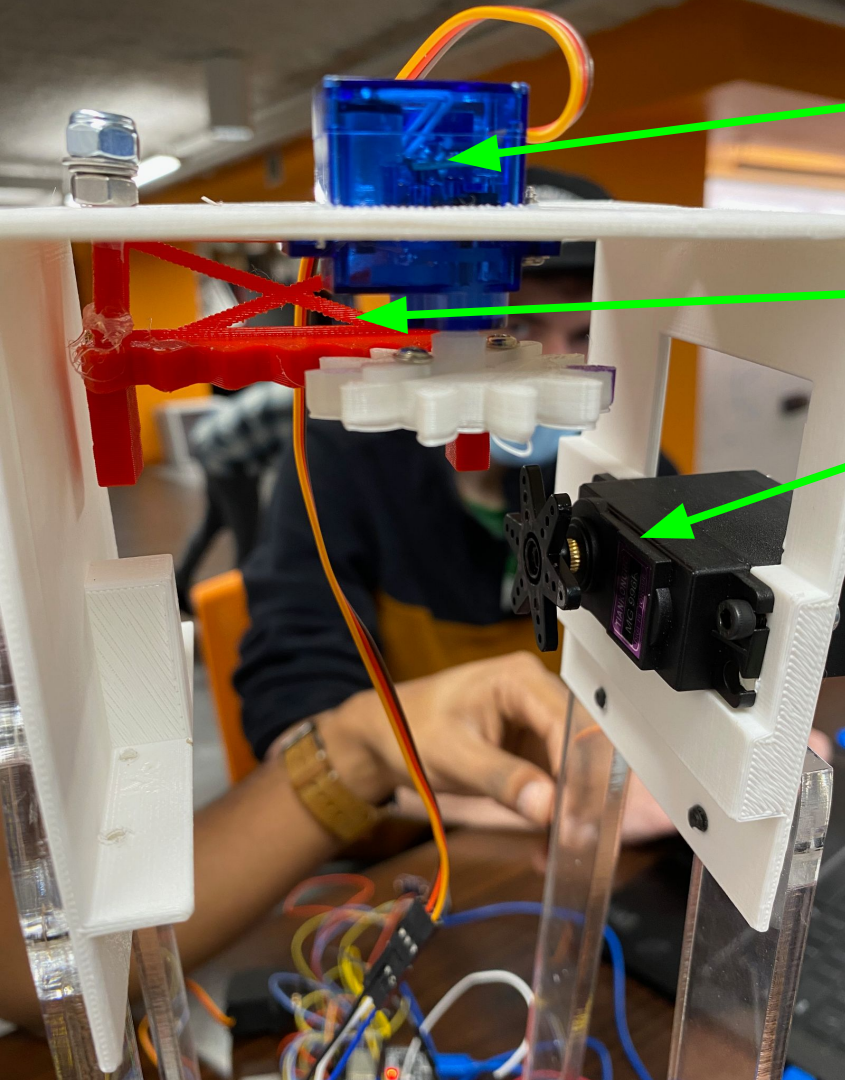
Main Assembly



- Storage for Raspberry Pi and ESP32
- Storage for Battery
- Decoupleable connection to servo horn
- Routing for power through the part
- Weight distributed evenly around the centerline for easier mechanics
- Through hole allows axel to support weight during operation and when decoupled

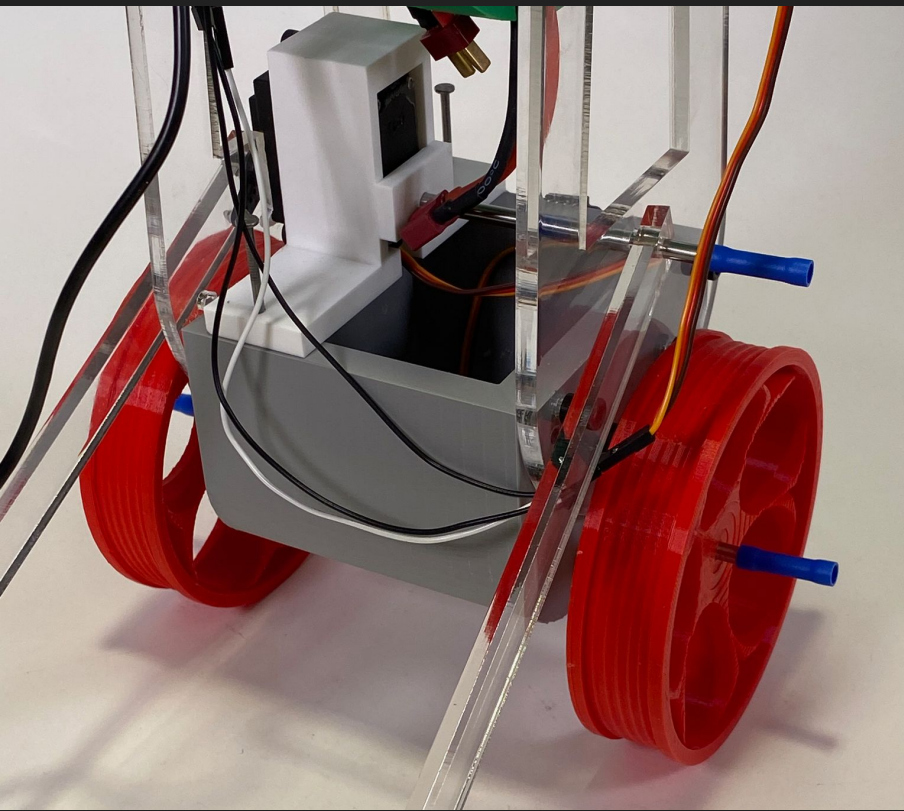


Pendulum Design



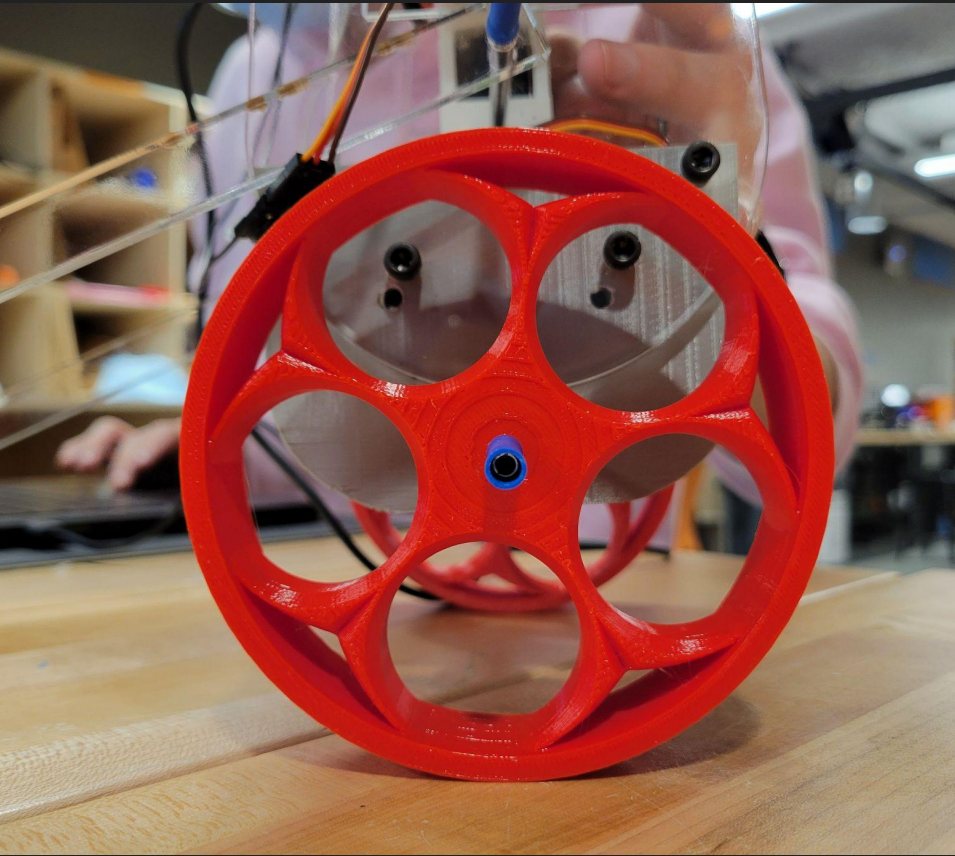
- Small servo drives the decoupling mechanism, prevents damage to servo when fully falling down
- Rack is designed to counteract moments with just one slot
- Large servo drives the pendulum and provides control input
- Vertical, narrow configuration allows robot to fall freely to $\pm 90^\circ$

Servo Box and Decoupling Mechanism



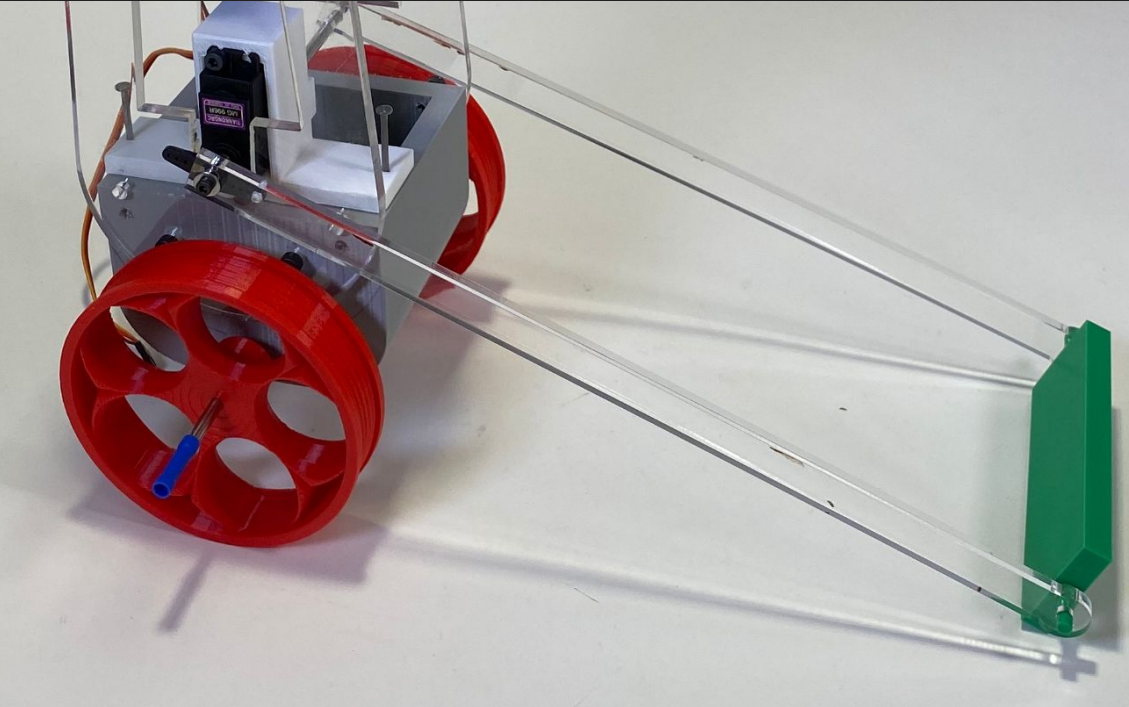
- Freewheel does not require any 360° servo motion or motors
- 3D printed body can be self-tapping, eliminating the need for loose hardware inside the box
- Wide wheel base helps prevent uncontrolled Y-axis motion
- Narrow, rounded box in the X-axis allows robot to fall to $\pm 90^\circ$ when unpowered

Wheel Box

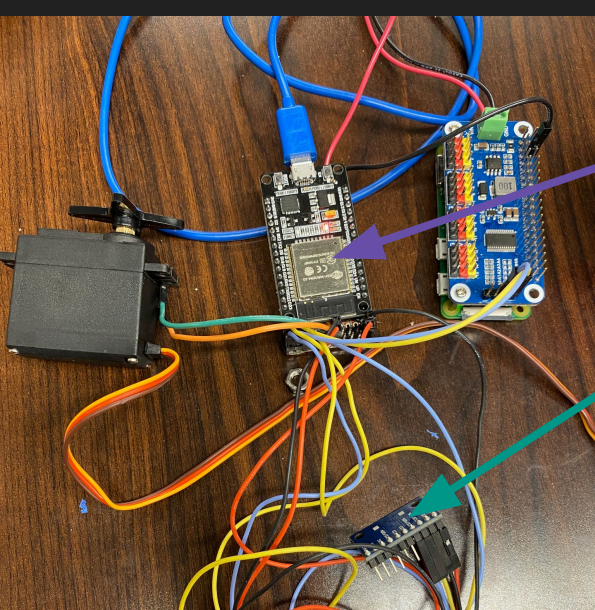


Wheels

Lifter Arm



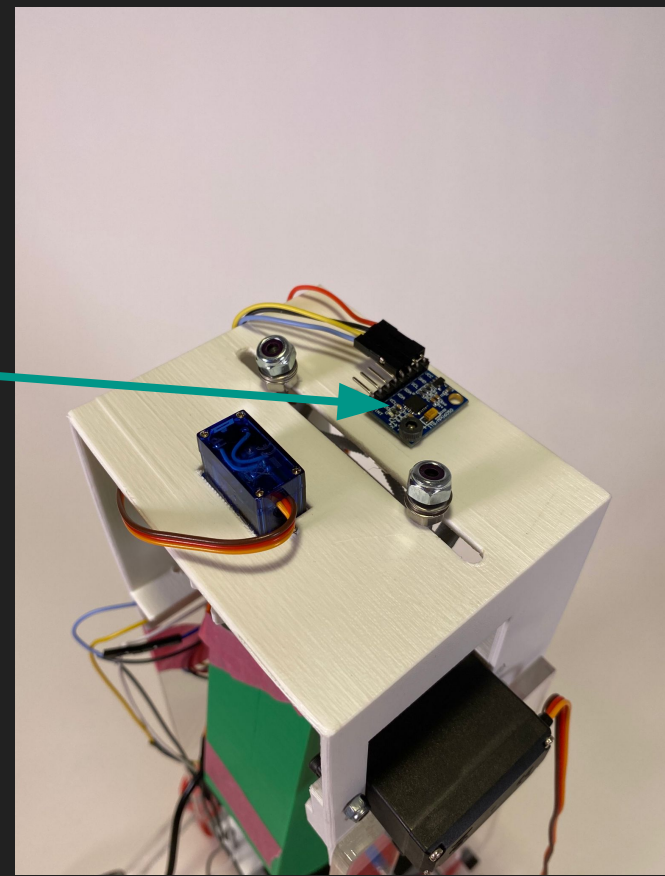
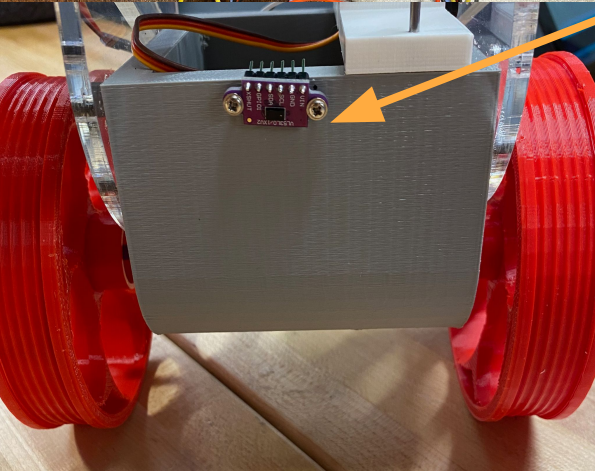
- Designed to lift the robot from a $\pm 90^\circ$ fall
- Works as a “kickstand” to allow the robot to balance when unpowered
- Second lifter servo would provide more power to lift the robot fully vertical



ESP32 provides rapid feedback control and sensing from IMU and LIDAR

IMU - MPU 6050 provides position & acceleration data for the robot body

LIDAR provides distance measurement and sensor fusion data during fall recovery



Control

Theoretical Control: Free Body Diagram and Equations of Motion

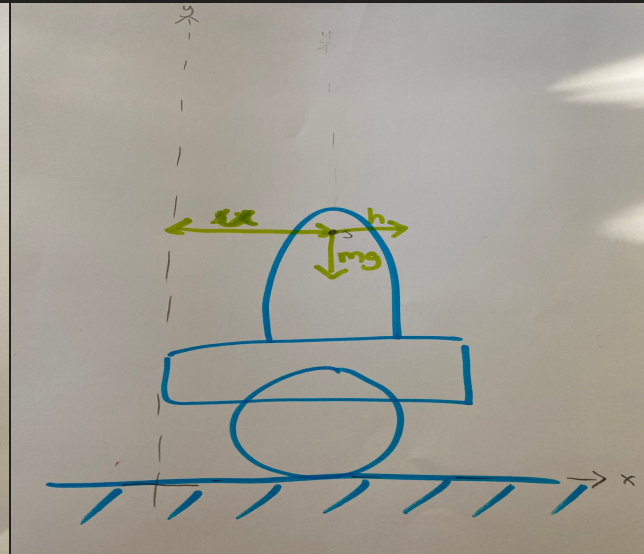
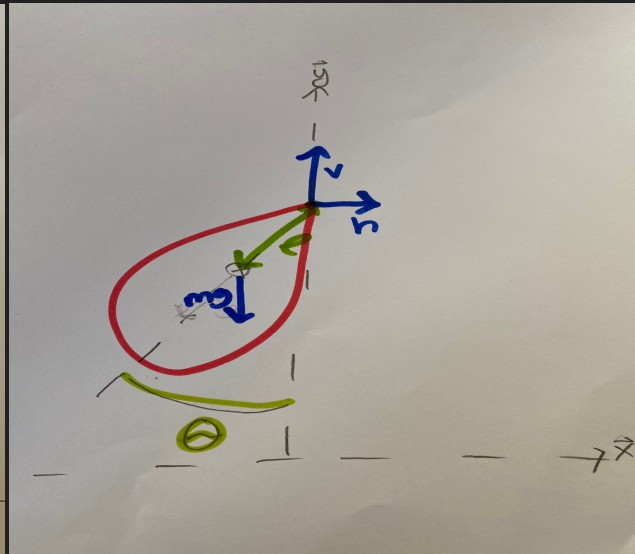
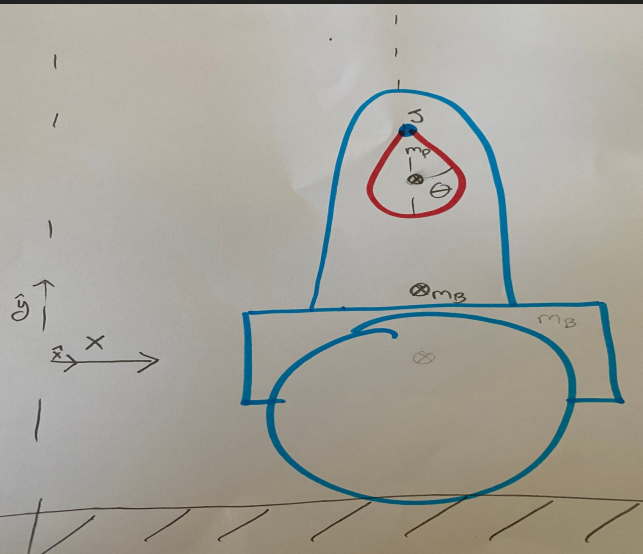
$$(M+m)x'' + ml\theta'' = u$$

$$Mlx'' + (I+ml^2)\theta'' - mgl\theta = 0$$

$$u = \cos(\alpha) / \text{height_robot}$$


$$\theta_p = (-m_p \cdot I_p \cdot \theta'' + (M_{\text{total}} \cdot I_p - M_{\text{total}} \cdot I_p) \cdot \theta'' + \mathit{math}.\cos(\alpha) \cdot h_{\text{robot}}) / (-g \cdot M_{\text{total}})$$

- Similar to cart and inverted pendulum
- Model pendulum as 30° circle segment for moment of inertia calculations
- Small angle assumption for pendulum control



Implemented Control System / Code

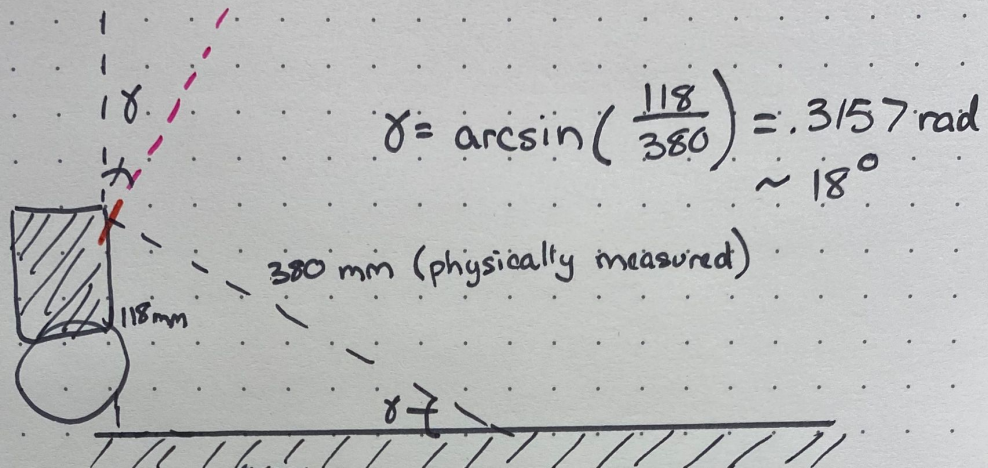
PID controller with data from the IMU



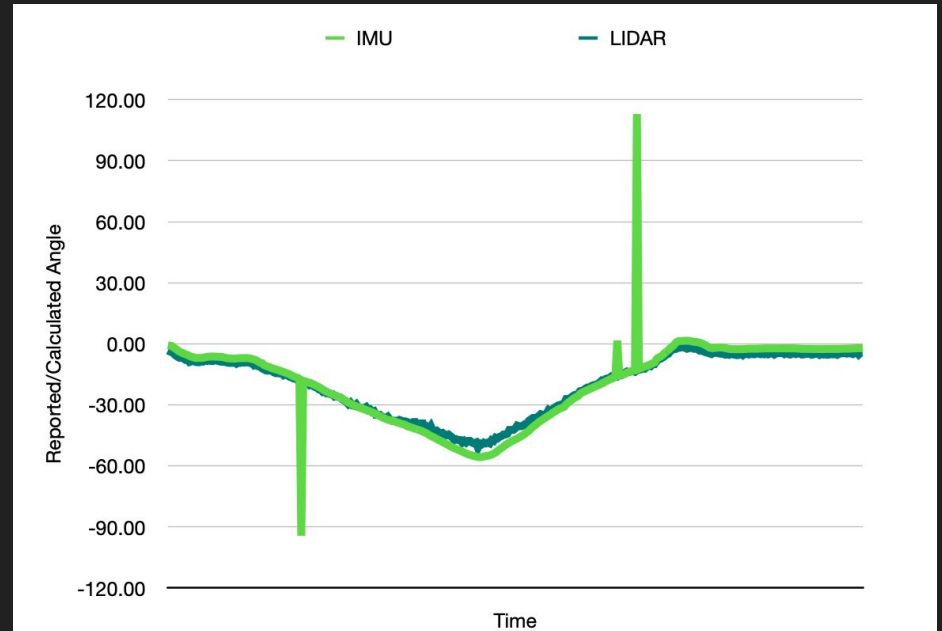
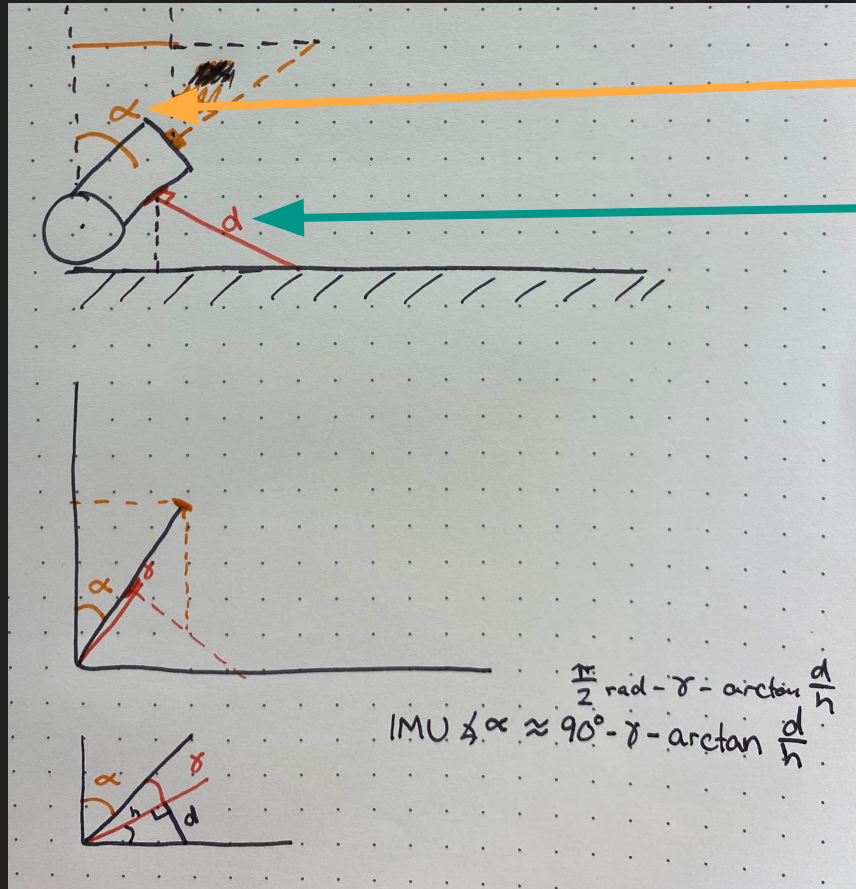
```
//////////////////////////////////PROPORTIONAL ERROR//////////////////////////////////
float pid_p = kp*error;
//////////////////////////////////INTERGRAL ERROR//////////////////////////////////
float pid_i = pid_i+(ki*error);
//////////////////////////////////DIFFERENTIAL ERROR//////////////////////////////////
float pid_d = kd*((error - previous_error)/elapsedTime);
//////////////////////////////////TOTAL PID VALUE//////////////////////////////////
PID = pid_p + pid_d + pid_i;
// Calculating the pulse we need to send to get the desired angle
float theta_p = (zero + (PID * ratio));
faboPWM.set_channel_value(15, theta_p);
```

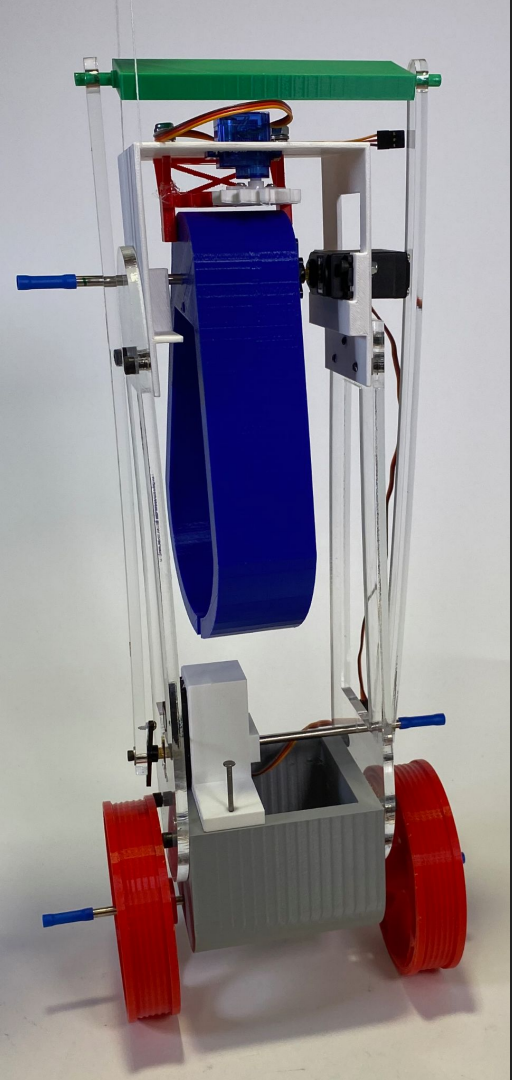
LIDAR vs IMU - measuring robot body angle

LIDAR is mounted approximately 18° from vertical on the wheel base front



LIDAR vs IMU - measuring robot body angle





Thank
You

